

# Analytical Formulation for Strength Prediction of orthogonal loaded, cold bonded Insert Load Introductions in Sandwich Elements

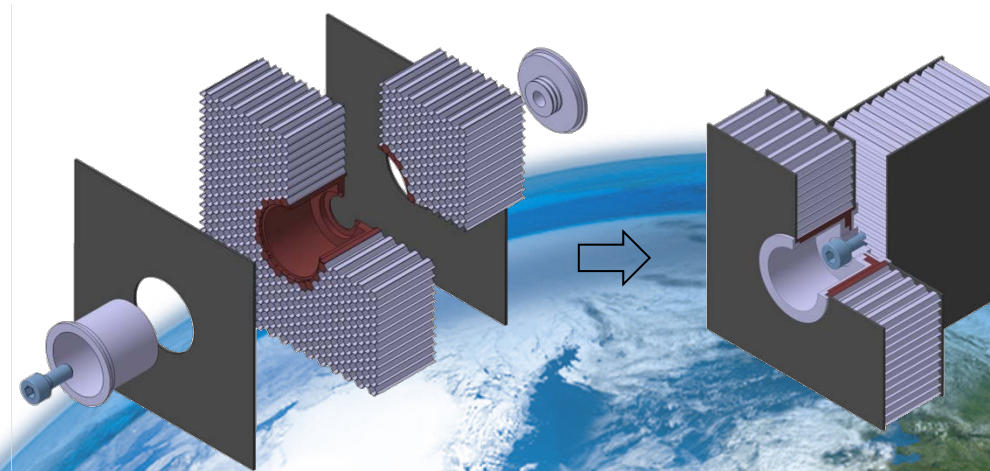
ICCS20, Paris

CNAM, 07.09.2017, Session "Sandwich Structures"

Room 21.3.23, 12h10

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**Department Composite Design**



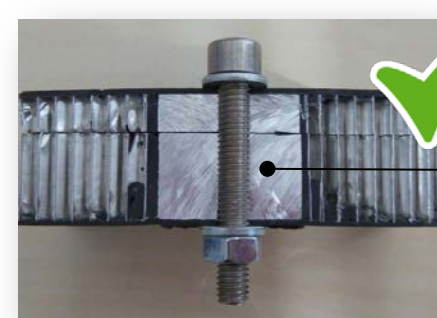
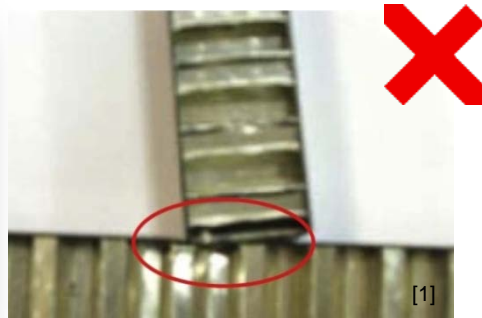
Knowledge for Tomorrow





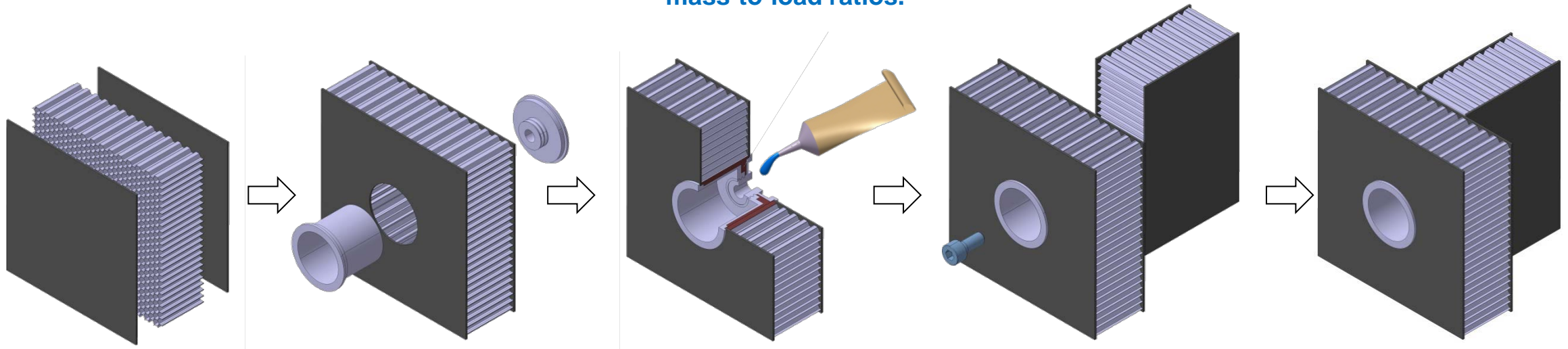
## 2. Problem task: Demand of Insert sizing Approach

### Why insert elements in sandwich structures?



Local core support element (“insert”) to resist the screw clamping force and to offer a smooth transition of structural loads into the adjacent sandwich structure.

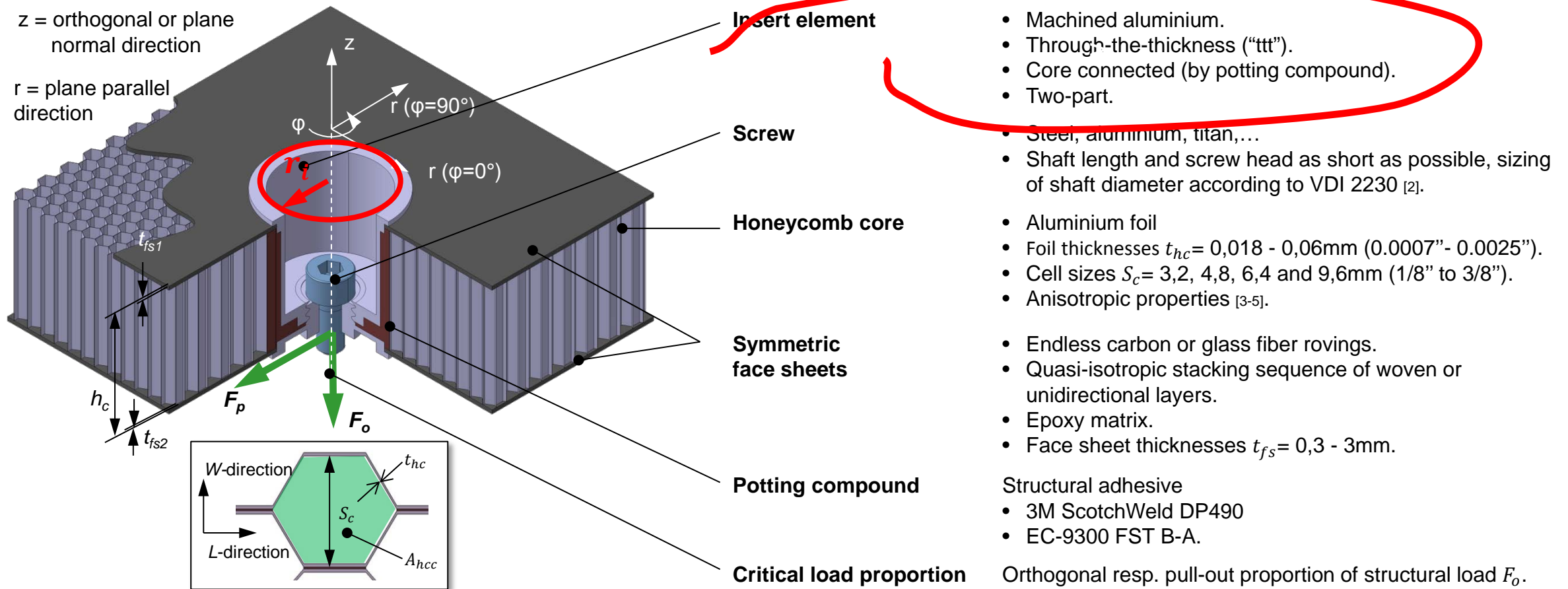
→ For detachable load introductions in sandwich elements, only connections with core support elements („inserts“) offer sufficient mass-to-load ratios.



→ Focussed: Cold-bonded, through-the-thickness insert elements with core connection via potting compound.

## 2. Problem task: Demand of Insert sizing Approach

### Specification: Basic Model

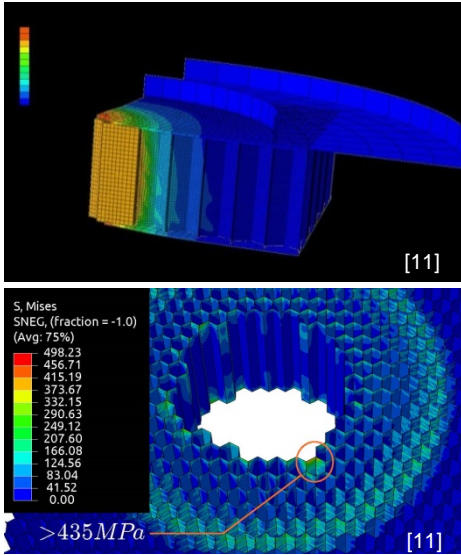
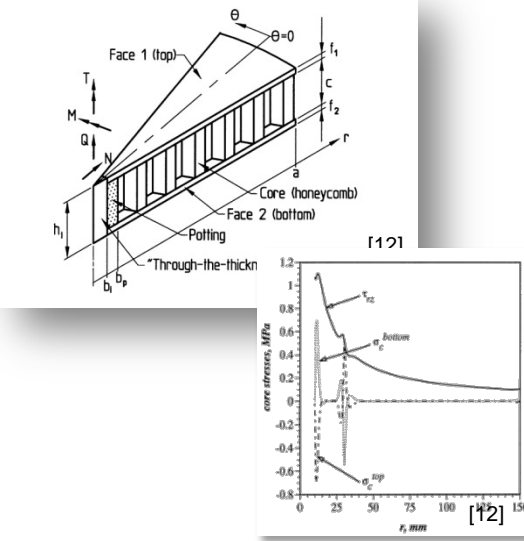
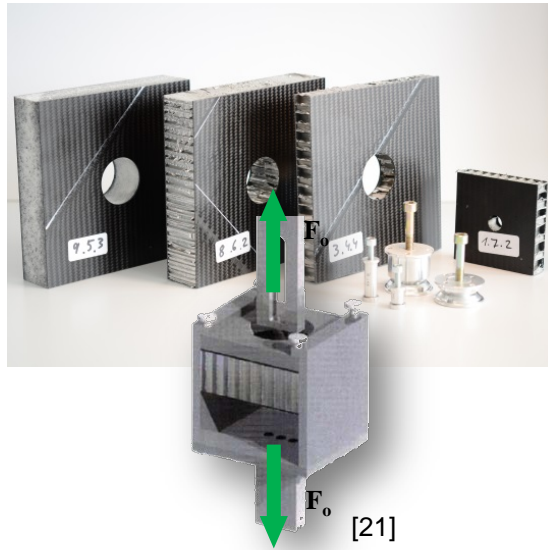



→ Screw and the insert element add the highest mass proportions, a minimization of the insert radius most beneficial!

→ Objective: Minimization of the insert element radius for a given maximal orthogonal load.

### 3. State of the Art

#### Insert load Introduction Description Methods

Simulation with FE-model	Higher order sandwich theory	Empirical approaches	“Simple” analytic theory
High resolution FE-modelling of individual insert load introductions [1-10].	Utilization of higher order sandwich plate theories (HSAPT) on (local) insert load introductions [12-18].	Testing of all necessary, differing insert element - sandwich configurations [19,20].	Sizing approach derived from failure / damage behavior [12-14, 24-27].
 <p>[11]</p>	 <p>[12]</p>	 <p>[21]</p>	 <p>[2016-09-21 067.JPG]</p> $\tau_{c,rz}(r,z) = \frac{Q_c}{A_c(r)}$ $\tau = \frac{F_{op} \cdot \eta_{ld}}{a_1 \cdot \tau_{c,rz,erit,eff} \cdot (t_{fs1} + h_c) \cdot 2\pi} - S_c \cdot \frac{r^2}{a_1^2}$
<b>Pro</b>	Precise results, evaluation of local phenomena is possible.		Simple and fast method on hand calculation level.
<b>Con</b>	Excessive effort for a sizing of numerous inserts exposed to various local conditions.		Less quality of results, not available for the relevant insert type.

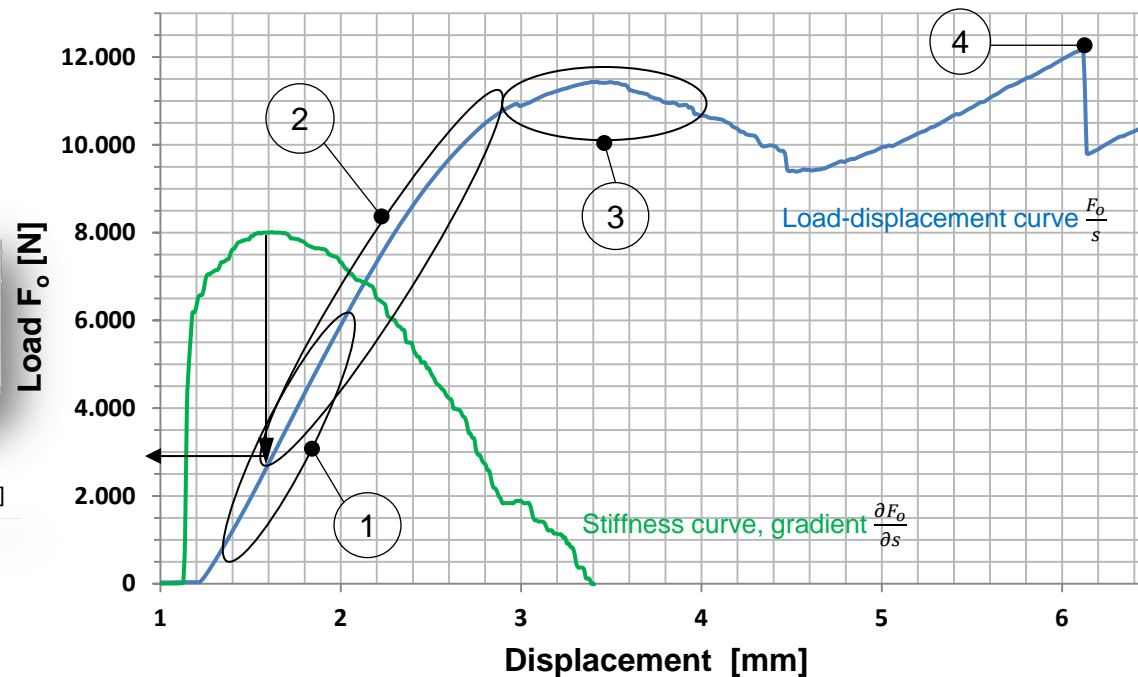
→ All models / theories, except from the simple analytical theory, are too complex for a sizing of numerous insert load introductions!



## 4. Insert sizing Approach

### Failure Behavior of ttt-Insert Load Introductions in Honeycomb Sandwich Elements

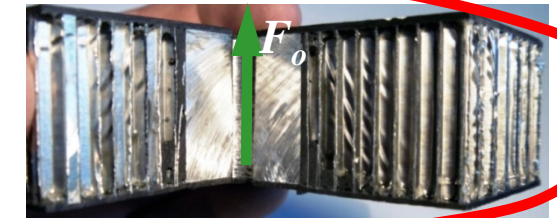
Typical load-deflection curve



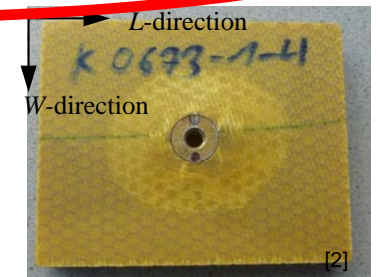
Damage characteristics of ttt-inserts

1. Elastic shear deformation of the core material near to the insert element

2. Irreversible resp. plastic shear deformation of core material.



3. Failure of core-face sheet bonding around the insert element, membrane formation of the face sheet.



4. Disintegration of insert element.

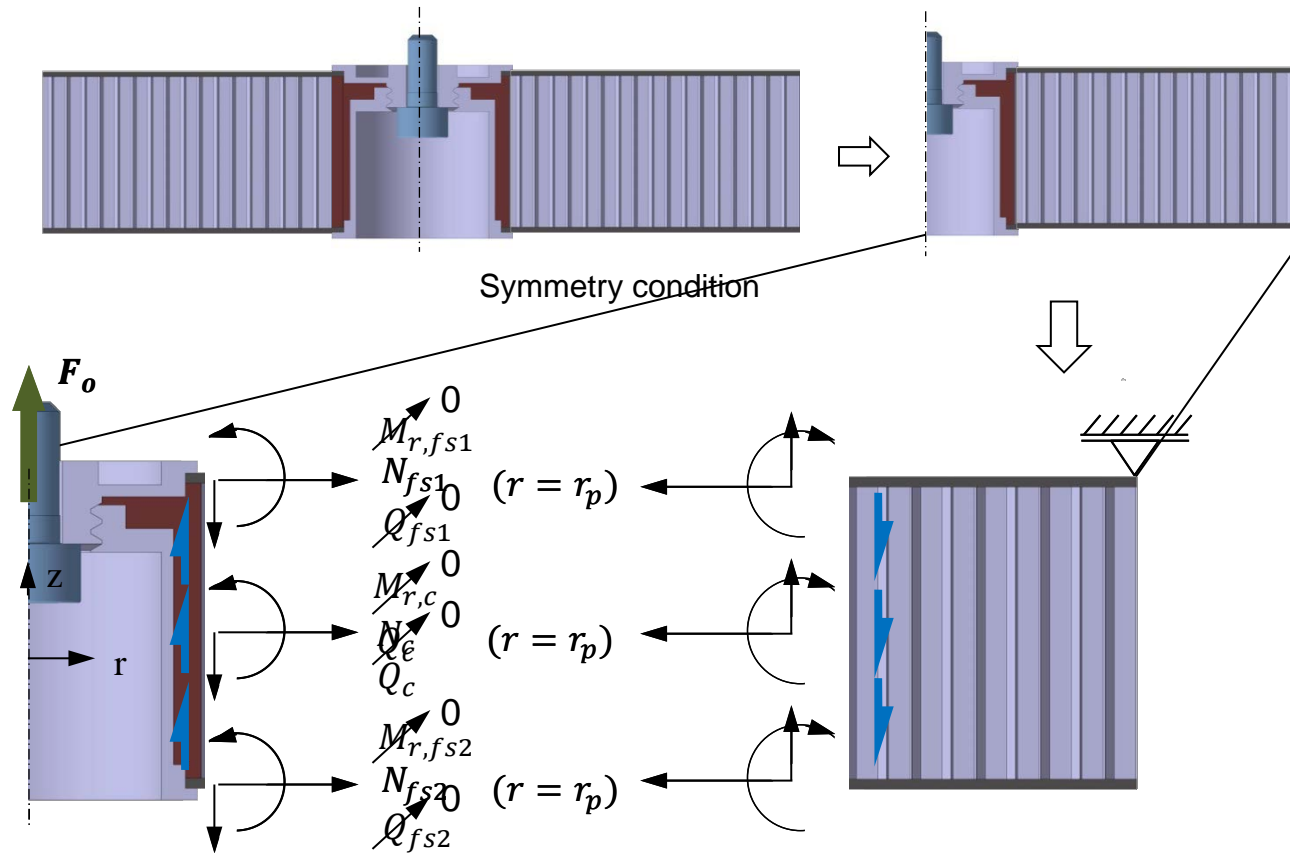


First relevant failure = Plastic core shear damage around the insert load introduction.

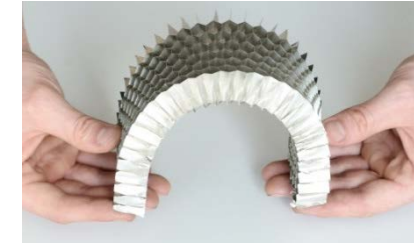
→ Request for the sizing formulation: No plastic core shear failure should occur until the limit load level  $F_o = F_{o,II}$ !

## 4. Insert sizing Approach

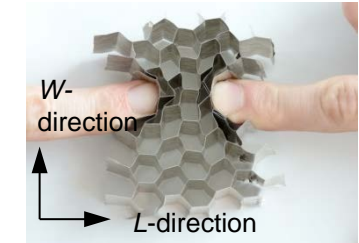
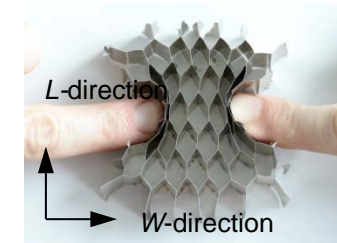
### Model Development: Basics, Honeycomb material Behavior



Free cut at junction between potting compound and honeycomb core ( $r = r_p(\varphi)$ ).



Bending resistance of honeycomb core  $\Downarrow \rightarrow M_{r,c} \approx 0$



Compression resistance of honeycomb core in  $r, \varphi$ -plane  $\Downarrow \rightarrow N_c \approx 0$



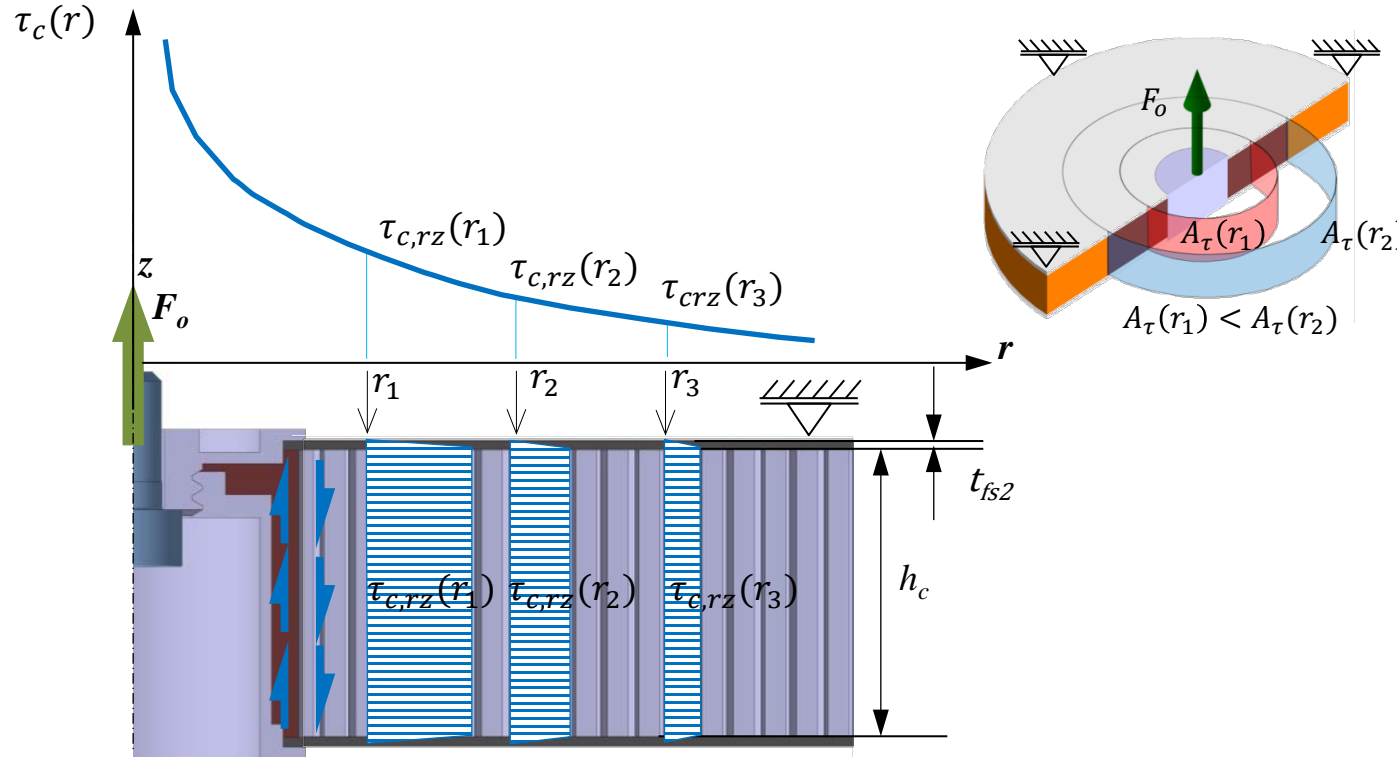
In case of face sheet bending resistance  $\Downarrow \rightarrow Q_{fs} \approx 0$ ,  $M_{r,fs} \downarrow$

→ For simplicity of the sizing approach, only the equilibrium of forces in the core are considered.

## 4. Insert sizing Approach

### Model Development: Local Core Shear Force, Stress and Area Relation

Relation between core shear force, core shear stress and shear area



Development of sizing formula:

$$\tau = \frac{Q}{A}$$



$$\tau_{c,rz}(r, z) = \frac{Q_c}{A_\tau(r)}$$



with  $A_\tau(r) = 2\pi \cdot r \cdot (t_{fs1} + h_c)$



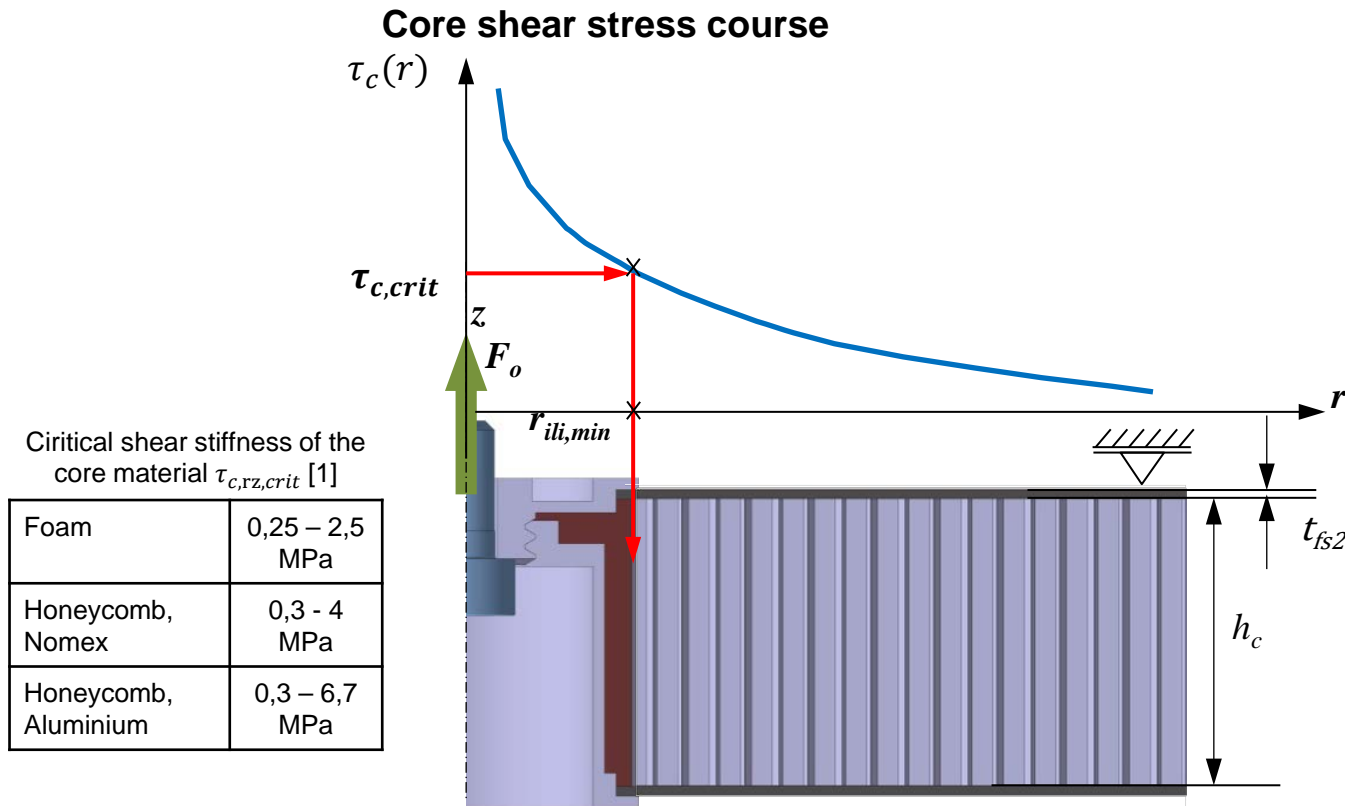
$$\tau_{c,rz}(r) = \frac{Q_c}{2\pi \cdot r \cdot (t_{fs1} + h_c)} \quad [1-4]$$

Approaching the insert load introduction, the core shear stress increases with  $1/r$  due to the decreasing effective shear area  $A_\tau(r)$ .



## 4. Insert sizing Approach

Basics: Core shear – pull out force relation: Development of sizing formula



**Approach:**

→ The extent of the insert load introduction must reach exactly to  $r = r_{ili,min}$ , where the local core shear stress  $\tau_{c,rz}(r)$  equals the core material shear strength  $\tau_{hc,crit}$ .

**Development of sizing formula:**

$$\tau_{c,rz}(r) = \frac{Q_c}{2\pi \cdot r \cdot (t_{fs} + h_c)}$$



$$r = \frac{Q_c}{\tau_{c,rz}(r) \cdot (t_{fs} + h_c) \cdot 2\pi}$$

At the location, where:

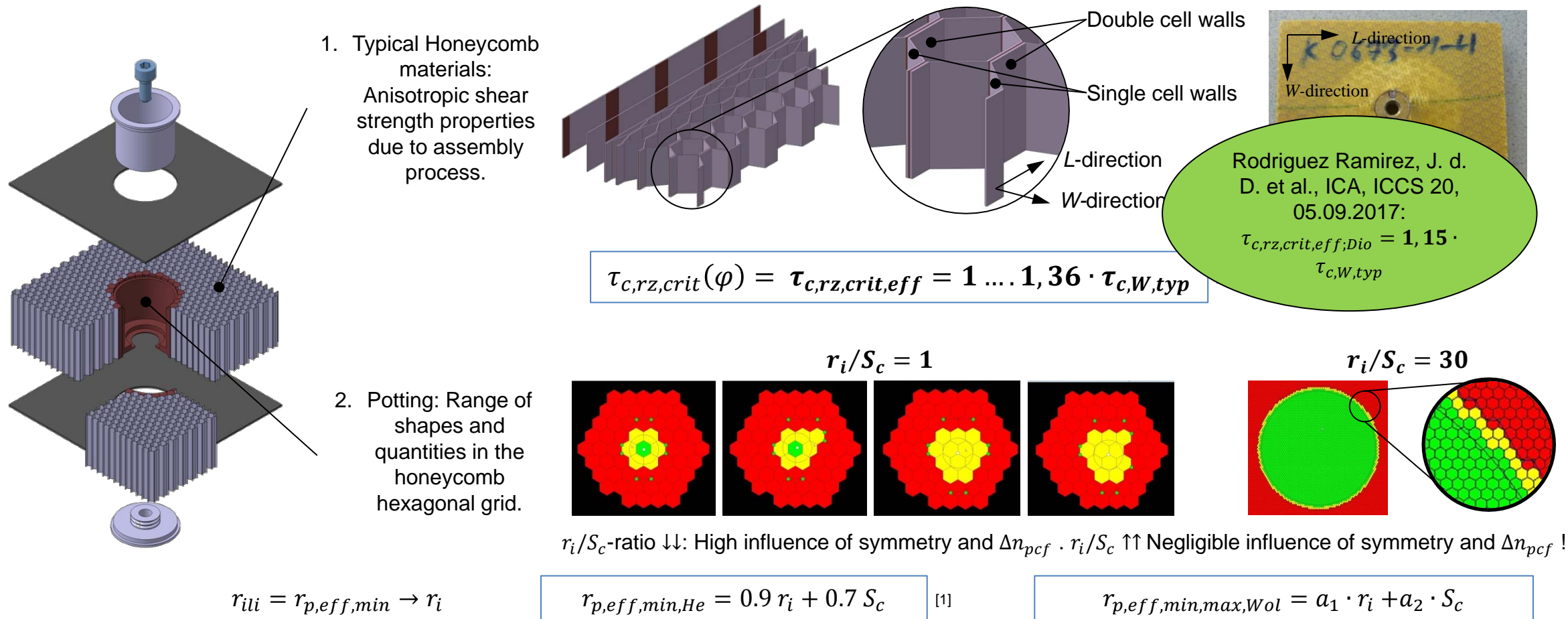
$$\tau_{c,rz}(r) = \tau_{c,rz,crit} \rightarrow r = r_{ili,min}$$

$r$  becomes:

$$r_{ili,min} = \frac{Q_{z,ll}}{\tau_{c,rz,crit} \cdot (t_{fs} + h_c) \cdot 2\pi} \quad [1-4]$$

## 4. Insert sizing Approach

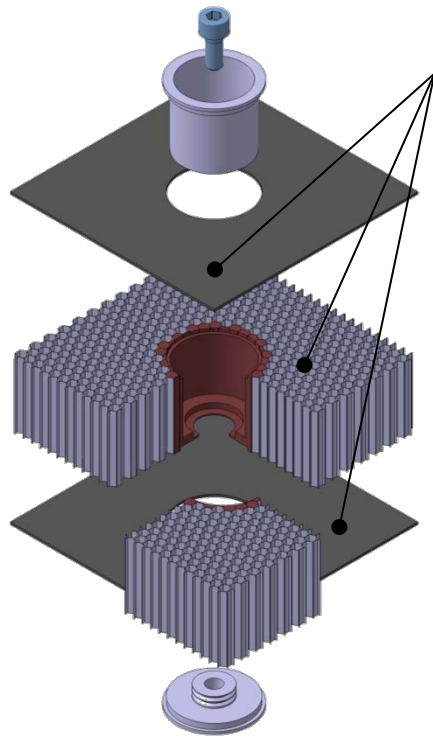
Influences on Load Carrying Capability: Anisotropic Honeycomb Material, Potting Shapes



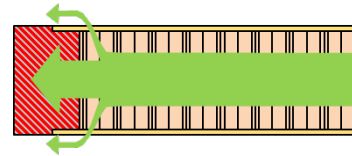
→ The anisotropic behavior of common honeycomb materials as well as the possible range of the potting must be respected!

## 4. Insert sizing Approach

### Influences on Load Carrying Capability: Sandwich: Geometry and Material Property Configurations



3. Varying core shear force proportions with different sandwich configurations.



VS.



→ High core-to-face sheet thickness ratio, low bending resistance of face sheets, high shear stiffness core of core material.

$$\eta_{ld} = 1 \quad [1,2]$$

→ Low core-to-face sheet thickness ratio, high bending resistance of face sheets, low shear stiffness of core material.

$$\eta_{ld} < 1 \quad [1,2]$$

$$r_{ili,min} = \frac{Q_{z,ll}}{\tau_{c,rz,crit} \cdot \left(t_{fs1} + \frac{h_c}{2}\right) \cdot 2\pi}$$



Final sizing formula respecting all crucial influences:

$$r_{i,min} = \frac{F_{op,ll} \cdot \eta_{ld}}{a_{1,min} \cdot \tau_{c,rz,crit,eff} \cdot (h_c + t_{fs}) \cdot 2\pi} - S_c \frac{a_{2,min}}{a_{1,min}}$$

→ There is actually no core shear force reduction factor  $\eta_{ld}$  available for the specific insert load introduction 'type' (ttt-, cold bonded insert load introduction)!

Validation?



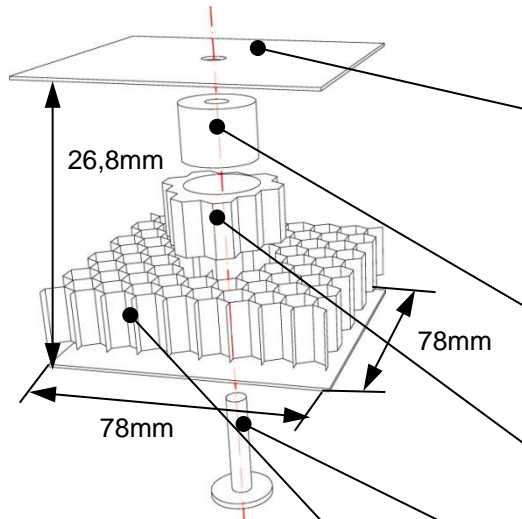
$$F_{o,ll,th} = \frac{r_{p,eff,rl} \cdot \tau_{c,rz,crit,eff} \cdot (h_c + t_{fs}) \cdot 2\pi}{\eta_{ld}}$$



## 5. Comparison of Test to analytic Results

### Test Definition: Specimen and Setup

#### Definition of test specimen for preliminary test



**Face sheets:** CFRP-PREPREG-panels with quasi-isotropic layup of 5 unidirectional and woven layers of endless carbon fiber T700 Torayca, epoxy matrix,  $t_{fs,1,2} = 0,85\text{mm}$ .

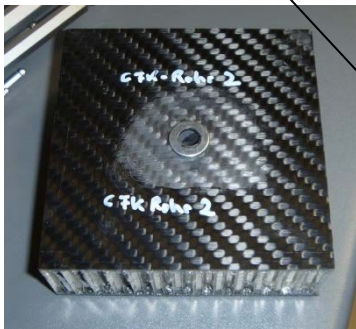
**Insert element:** Cylindrical tt-insert, core connected, machined aluminium,  $\varnothing = 26\text{mm}$  resp.  $r_i = 13\text{mm}$ .

**Potting compound:** Structural adhesive 3M ScotchWeld DP490.

**Screw:** M6 cylindrical head steel screw, grade 8.8, DIN ISO 4762.

**Honeycomb core:** Aluminium honeycomb, Plascore PAMG-XR1-4.5-1/8-10-P-5056,  $S_c = 3,2\text{mm}$ ,  $t_{hc} = 0,025\text{mm}$ ,  $\rho_c = 69\text{kg/dm}^3$ ,  $\tau_{c,rz,crit,W} = 1,18\text{MPa}$ ,  $h_c = 25\text{mm}$ . [1,2]

**Number of specimen:** 2

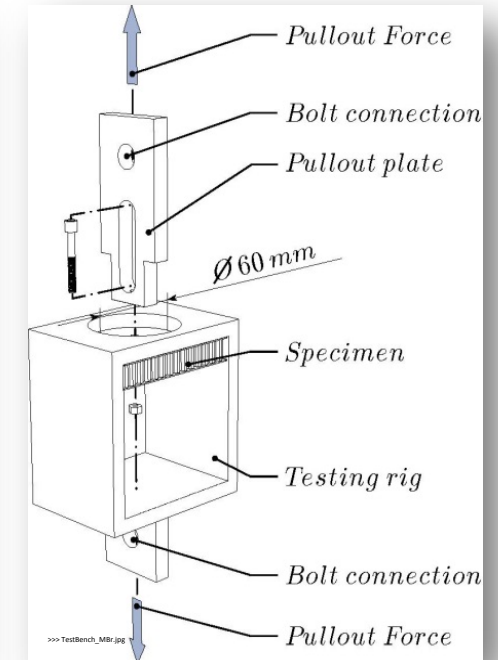


#### Test setup for orthogonal insert pull-out

##### Testing machine



##### Test rig



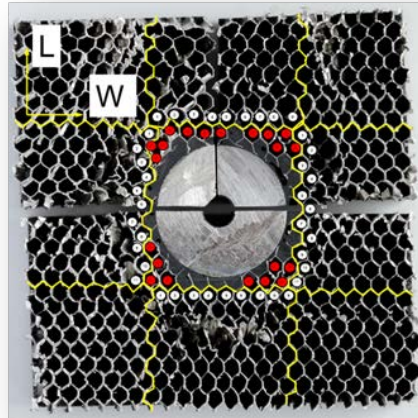
- Testing machine: Zwick/Roell BZ1
- Force transducer: 20kNZ0 WN 812616
- Data program: Zwick/Roell, TestExpert II

- Preload: 10N
- Testing speed: 6 mm/min
- Data rate: 10/sec

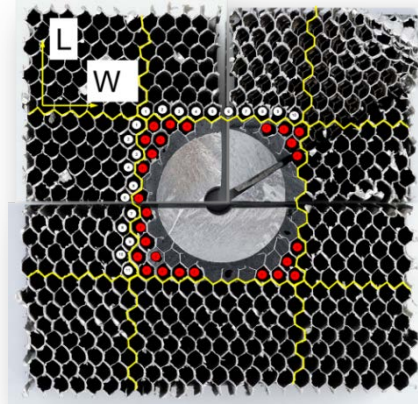
# 5. Comparison of Test to analytic Results

## Analytic Prediction with sizing Approach: Calculation

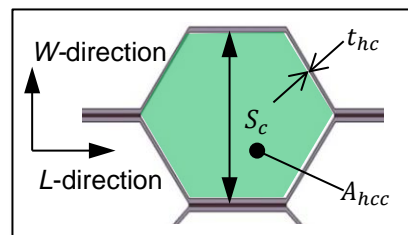
### 1. Real effective potting radius



Test specimen #1:  $n_{pcf,1} = 78$



Test specimen #2:  $n_{pcf,2} = 83$



$$r_{p,eff,rl} = \sqrt{\frac{n_{pfc} \cdot A_{hcc}}{\pi}} = \sqrt{\frac{n_{pfc} \cdot 3S_c^2}{\pi \cdot \sqrt{3}}} \quad [1]$$

$$r_{p,eff,rl,\#1} = 21,0mm$$

$$r_{p,eff,rl,\#2} = 21,6mm$$

### 2. Calculation of homogenized honeycomb shear strength

$$\tau_{c,crit,eff,Heimbs} = \tau_{c,crit,W} \quad [2]$$

$$\tau_{hc,rz,crit,eff,Hei} = 1,18MPa$$

$$\tau_{c,crit,eff,Hertel} = 1,36 \cdot \tau_{c,crit,W} \quad [1]$$

$$\tau_{c,rz,crit,eff,Her} = 1,6MPa$$

### 3. Rearrangement of sizing formulation, calculation of theoretic critical first failure load

$$F_{o,ll,th} = \frac{r_{p,eff,rl} \cdot \tau_{c,rz,crit,eff,i} \cdot (h_c + t_{fs}) \cdot 2\pi}{\eta_{ld}}$$

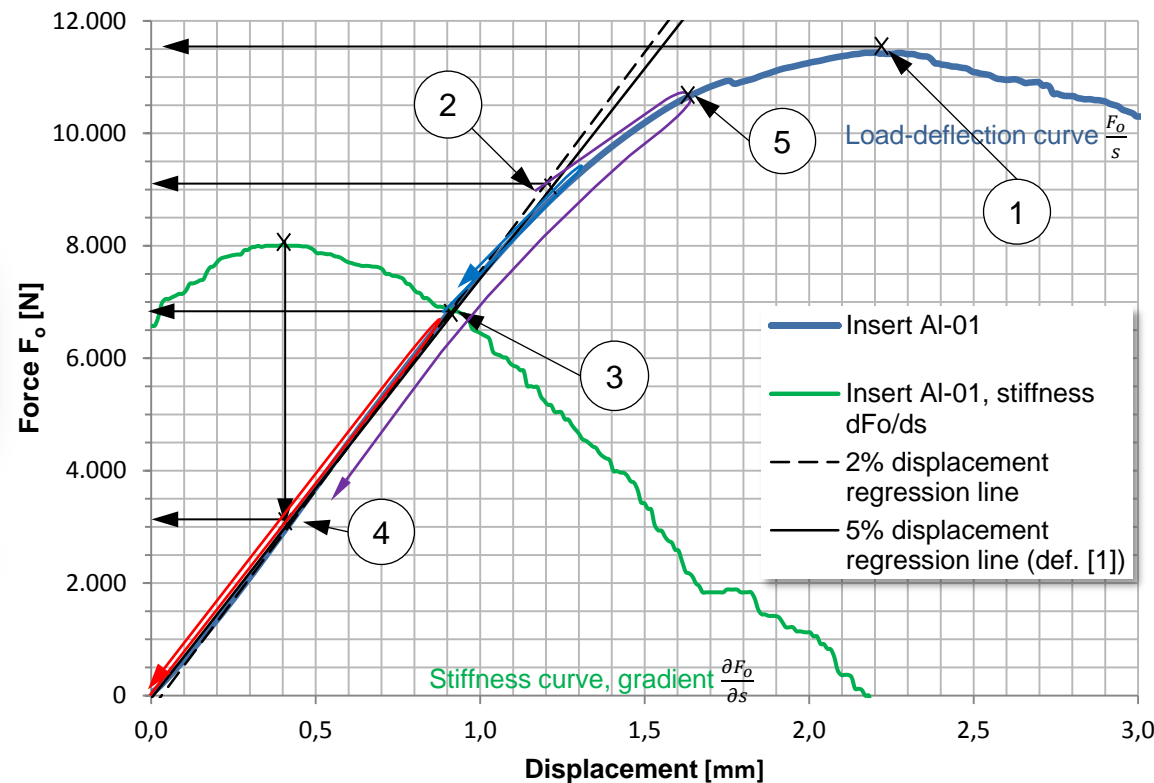
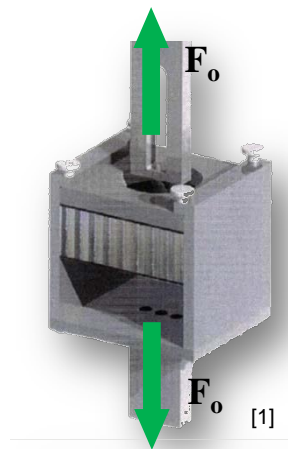
$$F_{o,ll,th,\#1} = \frac{21,0mm \cdot 1,6 N/mm^2 \cdot (25mm + 0,85mm) \cdot 2\pi}{1} = 5457N$$

$$F_{o,ll,th,\#1} = \frac{21,6mm \cdot 1,6 N/mm^2 \cdot (25mm + 0,85mm) \cdot 2\pi}{1} = 5638N$$

# 5. Comparison of Test to analytic Results

## Divergent Test Data Interpretations

→ Which characteristic of the stiffness curve is to allocate to the first plastic core shear failure?



Five different methods of first failure load level allocation are common:

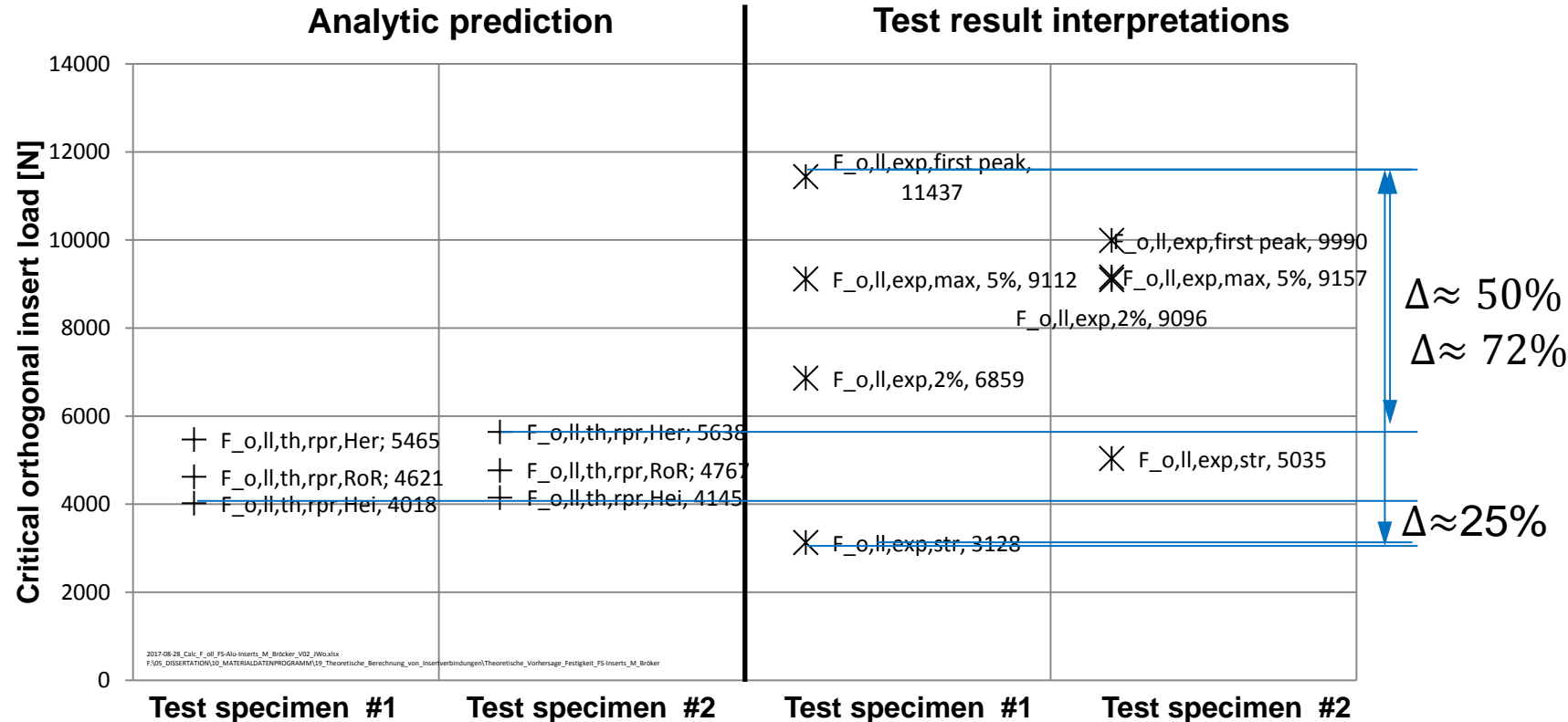
1. First peak. [1-8]  $F_{o,ll,exp,fp,\#1} = 11437N$
2. Intersection with 5% displacement regression line. [10]  $F_{o,ll,exp,5\%,\#1} = 9112N$
3. Intersection with 2% displacement regression line. [9]  $F_{o,ll,exp,2\%,\#1} = 6859N$
4. Point of maximal stiffness.  $F_{o,ll,exp,str,\#1} = 3128N$
5. Analysis of hysteresis tests. [11-12]

→ Several “state of the art” first irreversible failure interpretations deliver highly diverging results...



## 5. Comparison of Test to analytic Results

Deviations between theoretical and practical Results



Theoretical values considering the individual real potting radii  $r_{p,b,1,2}$  and  $\Delta\tau_{hc,crit,eff}$  from different core shear approaches.

Test results considering different methods of critical load level interpretations.

1. Way too high divergences between different **test result interpretations**: Which one represents the first irreversible failure?
2. The minimal test result (“maximal stiffness point” failure interpretation) of specimen #1 is smaller than the minimal analytic prediction.  
→ **Danger of critical overestimation by the analytic prediction!**
3. Analytic results compared to “first peak” and “5% regression line” failure test interpretations. → Much too conservative results due to underestimation, **danger of an oversizing of the insert load introduction!**

→ In their actual forms, neither the analytical approach nor the test evaluation are sufficient for an effective sizing of insert elements!

## 6. Way forward

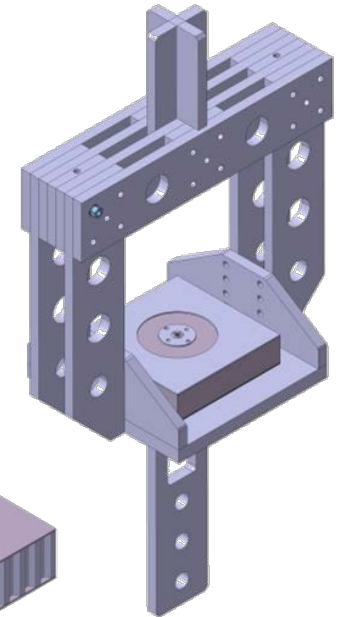
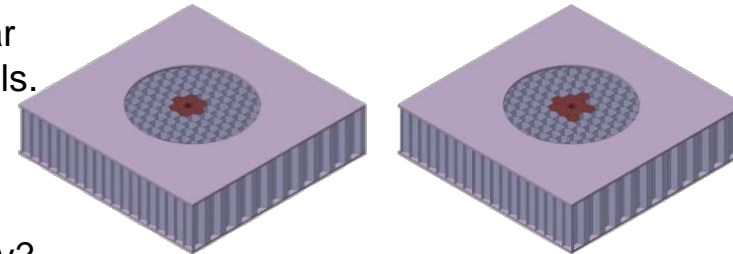
**Issue #1:** Different first failure load level interpretations of test results.

1. Improved test procedure by hysteresis tests and cutting samples → Deduction of improved test data interpretation process.



**Issue #2:** Divergent core shear homogenization approaches.

2. Tests with special specimen with locally removed face sheets: Observation of shear damage process of individual core cell walls.
  - Support of improved test data interpretation process.
  - Is it possible to measure the effective core shear strength ( $\tau_{c,crit,eff}$ ) directly?



**Issue #3:** No shear force reduction factor  $\eta_{ld}$  for the certain insert configuration!

3. Deduction of correct core shear force reduction factor  $\eta_{ld}$  for the certain insert type with the help of the higher order sandwich plate theory (HSAPT).

$$\eta_{ld} = f(h_c, t_{fs}, G_{c,W,typ}, E_{fs,eff}, \nu_{fs}, r_{spprt}, \dots)$$

→ Three main measures to counteract the large discrepancies of theoretical to test results!



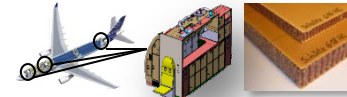
# Thanks for your Attention!

Dipl.-Ing. Johannes Wolff  
German Aerospace Centre (DLR)

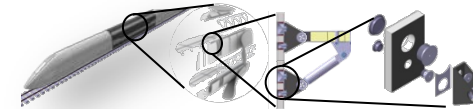
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Adaptive Systems (FA)  
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D-38108 Braunschweig

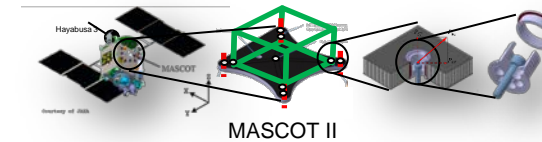
Phone: +49 531 295 - 2343  
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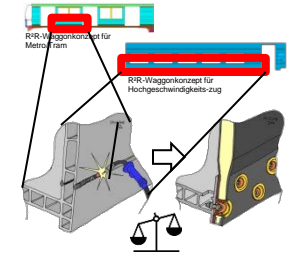
Innovative Galley (InGa)



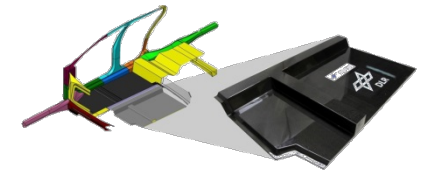
Next Generation Train Project (NGT II - III)



MASCOT II



Roll to Rail-Project (R2R)



Endkonturne Volumenbauteile (EVo),  
Machbarkeitsstudie Sandwichboden (EVo MSB)

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